

Addition, Subtraktion: Aufgabe 4



Man vereinfache so weit wie möglich

$$a) \quad \frac{1}{a} + \frac{2}{b} + \frac{1}{c}$$

$$b) \quad \frac{1}{ab} + \frac{1}{ac} + \frac{1}{bc}$$

$$c) \quad \frac{b - 4a}{a + b} + \frac{2a^2 + 5ab + 3b^2}{(a + b)^2} - 1$$

$$d) \quad \frac{a}{b^2c} + \frac{c}{ab^2} - \frac{2}{b^2}$$

$$e) \quad \frac{3}{a - 1} + \frac{6}{1 - a^2} - \frac{5}{a + 1}$$

$$a) \quad \frac{1}{a} + \frac{2}{b} + \frac{1}{c} = \frac{bc + 2ac + ab}{abc}$$

$$b) \quad \frac{1}{ab} + \frac{1}{ac} + \frac{1}{bc} = \frac{a + b + c}{abc}$$

$$c) \quad \frac{b - 4a}{a + b} + \frac{2a^2 + 5ab + 3b^2}{(a + b)^2} - 1 = -\frac{3(a - b)}{a + b}$$

$$d) \quad \frac{a}{b^2c} + \frac{c}{ab^2} - \frac{2}{b^2} = \frac{(a - c)^2}{ab^2c}$$

$$e) \quad \frac{3}{a - 1} + \frac{6}{1 - a^2} - \frac{5}{a + 1} = -\frac{2}{a + 1}$$

Addition, Subtraktion: Aufgabe 5



Man vereinfache so weit wie möglich

$$a) \quad \frac{a}{x^2 - a^2} - \frac{x + a}{x - a} + \frac{x - a}{x + a}$$

$$b) \quad \frac{a}{x^2 - a^2} - \frac{2x}{x - a} - \frac{a - x}{x + a}$$

$$c) \quad \frac{1}{x} - \frac{1}{y} + \frac{x - y}{xy} - \frac{(x + y)^2}{xy}$$

$$d) \quad \frac{1 + x}{1 - x} - \frac{1 - x}{1 + x} + \frac{2x}{1 - x^2}$$

$$e) \quad \frac{4x + 1}{x - 1} - \frac{3x - 2}{x + 2} - \frac{x(x + 14)}{(x - 1)(x + 2)}$$

$$f) \quad \frac{9x + 5}{x^2 - 1} - \frac{7x + 4}{x^2 - x} - \frac{2(x - 2)}{x^2 + x} + 1$$

Addition, Subtraktion: Lösung 5

$$a) \quad \frac{a}{x^2 - a^2} - \frac{x + a}{x - a} + \frac{x - a}{x + a} = \frac{a(4x - 1)}{(x + a)(x - a)}$$

$$b) \quad \frac{a}{x^2 - a^2} - \frac{2x}{x - a} - \frac{a - x}{x + a} = \frac{a + a^2 - 4ax - x^2}{(x + a)(x - a)}$$

$$c) \quad \frac{1}{x} - \frac{1}{y} + \frac{x - y}{xy} - \frac{(x + y)^2}{xy} = -\frac{(x + y)^2}{xy}$$

$$d) \quad \frac{1 + x}{1 - x} - \frac{1 - x}{1 + x} + \frac{2x}{1 - x^2} = \frac{6x}{1 - x^2}$$

$$e) \quad \frac{4x + 1}{x - 1} - \frac{3x - 2}{x + 2} - \frac{x(x + 14)}{(x - 1)(x + 2)} = 0$$

$$f) \quad \frac{9x + 5}{x^2 - 1} - \frac{7x + 4}{x^2 - x} - \frac{2(x - 2)}{x^2 + x} + 1 = \frac{x^3 - x - 8}{x^3 - x}$$

Bruchrechnung: Aufgabe 6



In den Nennern der folgenden Brüche sind die Wurzeln zu beseitigen:

Beispiel:

$$\begin{aligned}\frac{1 - \sqrt{2}}{1 + \sqrt{2}} &= \frac{(1 - \sqrt{2})^2}{(1 + \sqrt{2})(1 - \sqrt{2})} = \frac{1 - 2\sqrt{2} + (\sqrt{2})^2}{1 - (\sqrt{2})^2} = \\ &= \frac{3 - 2\sqrt{2}}{-1} = 2\sqrt{2} - 3\end{aligned}$$

$$a) \frac{2 + \sqrt{2}}{\sqrt{2}}$$

$$b) \frac{a + b}{\sqrt{a} - \sqrt{b}} \quad (a, b \geq 0, a \neq b)$$

$$c) \frac{1 + \sqrt{3}}{2\sqrt{3} + 3\sqrt{2}}, \quad d) \frac{1 + \sqrt{2} - \sqrt{3}}{1 - \sqrt{2} + \sqrt{6}}$$

$$e) \frac{\sqrt{3} - \sqrt{2}}{\sqrt{2} + \sqrt{3} - \sqrt{8}}$$

Addition, Subtraktion: Lösung 6

$$a) \frac{2 + \sqrt{2}}{\sqrt{2}} = \frac{(2 + \sqrt{2})\sqrt{2}}{2} = 1 + \sqrt{2}$$

$$b) \frac{a + b}{\sqrt{a} - \sqrt{b}} = \frac{(a + b)(\sqrt{a} + \sqrt{b})}{a - b}$$

$$c) \frac{1 + \sqrt{3}}{2\sqrt{3} + 3\sqrt{2}} = \frac{(1 + \sqrt{3})(2\sqrt{3} - 3\sqrt{2})}{(2\sqrt{3} + 3\sqrt{2})(2\sqrt{3} - 3\sqrt{2})} = \\ = -1 + \frac{\sqrt{2}}{2} - \frac{\sqrt{3}}{3} + \frac{\sqrt{6}}{2}$$

$$d) \frac{1 + \sqrt{2} - \sqrt{3}}{1 - \sqrt{2} + \sqrt{6}} = 15 - 11\sqrt{2} + 9\sqrt{3} - 6\sqrt{6}$$

Hinweis:
$$\frac{1 + \sqrt{2} - \sqrt{3}}{1 - \sqrt{2} + \sqrt{6}} = \frac{(1 + \sqrt{2} - \sqrt{3})(1 - \sqrt{2} - \sqrt{6})}{(1 - \sqrt{2})^2 - 6}$$

$$e) \frac{\sqrt{3} - \sqrt{2}}{\sqrt{2} + \sqrt{3} - \sqrt{8}} = \frac{\sqrt{3} - \sqrt{2}}{\sqrt{2} + \sqrt{3} - 2\sqrt{2}} = 1$$

Bruchrechnung: Aufgabe 7



In den Nennern der folgenden Brüche sind die Wurzeln zu beseitigen:

$$a) \frac{2\sqrt{3}}{\sqrt{2} + \sqrt{3} + \sqrt{5}}$$

$$b) \frac{1}{2 + \sqrt{2} + \sqrt{3} + \sqrt{6}}$$

$$\begin{aligned} a) \quad \frac{2\sqrt{3}}{\sqrt{2} + \sqrt{3} + \sqrt{5}} &= \frac{2\sqrt{3} (\sqrt{2} + \sqrt{3} - \sqrt{5})}{(\sqrt{2} + \sqrt{3} + \sqrt{5}) (\sqrt{2} + \sqrt{3} - \sqrt{5})} = \\ &= \frac{2\sqrt{3} (\sqrt{2} + \sqrt{3} - \sqrt{5})}{(\sqrt{2} + \sqrt{3})^2 - (\sqrt{5})^2} = \frac{2\sqrt{3} (\sqrt{2} + \sqrt{3} - \sqrt{5})}{(\sqrt{2})^2 + 2\sqrt{2} \cdot \sqrt{3} + (\sqrt{3})^2 - (\sqrt{5})^2} = \\ &= \frac{1}{\sqrt{2}} (\sqrt{2} + \sqrt{3} - \sqrt{5}) = \frac{1}{2} (2 + \sqrt{6} - \sqrt{10}) \end{aligned}$$

$$\begin{aligned} b) \quad \frac{1}{2 + \sqrt{2} + \sqrt{3} + \sqrt{6}} &= \frac{2 + \sqrt{2} - (\sqrt{3} + \sqrt{6})}{(2 + \sqrt{2} + \sqrt{3} + \sqrt{6}) (2 + \sqrt{2} - (\sqrt{3} + \sqrt{6}))} = \\ &= \sqrt{6} + \sqrt{2} - \sqrt{3} - 2 \end{aligned}$$