

$$\frac{\partial f}{\partial x} = \frac{2}{x} (3 \ln$$

$$\frac{\partial f}{\partial y} = \bar{y} (-\ln y -$$

Partielle Ableitungen: Schriftliche Arbeit 3

Partielle Ableitungen: Aufgabe

Bestimmen Sie die partiellen Ableitungen 1. Ordnung
der Funktion f

$$1) \ f(x, y) = (\sqrt{x} - y^3) e^{-2y}$$

$$2) \ f(x, y) = \ln\left(\frac{x^3}{4y}\right) - e^{-y^2}$$

$$3) \ f(x, y, z) = \ln\left(\frac{y\sqrt{z}}{x^2}\right) + e^{x-z}$$

$$4) \ f(x, y) = e^{\cos x} + y \sin(e^x)$$

$$5) \ f(x, y) = e^{\ln z - xz}$$

Partielle Ableitungen: Lösungen 1, 3

$$1) \quad f(x,y) = (\sqrt{x} - y^3) e^{-2y} = \sqrt{x} \cdot e^{-2y} - y^3 e^{-2y}$$

$$\frac{\partial f}{\partial x} = \frac{1}{2\sqrt{x}} \cdot e^{-2y} \quad , \quad \frac{\partial f}{\partial y} = \sqrt{x} \cdot (-2)e^{-2y} - (3y^2 e^{-2y} + y^3 e^{-2y}(-2)) \\ = e^{-2y}(-2\sqrt{x} - 3y^2 + 2y^3)$$

$$3) \quad f(x,y,z) = \ln\left(\frac{y\sqrt{z}}{x^2}\right) + e^{x-z} \\ = \ln y + \frac{1}{2} \ln z - 2 \ln x + e^{x-z}$$

$$\frac{\partial f}{\partial x} = -\frac{2}{x} + e^{x-z}$$

$$\frac{\partial f}{\partial y} = \frac{1}{y}, \quad \frac{\partial f}{\partial z} = \frac{1}{2z} - e^{x-z}$$

Partielle Ableitungen: Lösungen 2, 4

$$2) f(x,y) = \ln\left(\frac{x^3}{4y}\right) - e^{y^2} = \\ = \ln(x^3) - \ln(4y) - e^{y^2} = 3\ln x - (\ln 4 + \ln y) - e^{y^2} = \\ = 3\ln x - \ln 4 - \ln y - e^{y^2}$$

$$\frac{\partial f}{\partial x} = \frac{\partial}{\partial x} (3\ln x) = 3 \frac{\partial}{\partial x} (\ln x) = \frac{3}{x},$$

$$\frac{\partial f}{\partial y} = \frac{\partial}{\partial y} (-\ln y - e^{y^2}) = -\frac{1}{y} - 2ye^{y^2}$$

$$4) f(x,y) = e^{\cos x} + y \cdot \sin(e^x)$$

$$\frac{\partial f}{\partial x} = e^{\cos x} \frac{\partial}{\partial x} (\cos x) + y \cdot \frac{\partial}{\partial x} (\sin(e^x)) = -\sin x \cdot e^{\cos x} + y \cdot \cos(e^x) \cdot e^x = \\ = -\sin x \cdot e^{\cos x} + y \cdot e^x \cdot \cos(e^x)$$

$$\frac{\partial f}{\partial y} = \sin(e^x) \frac{\partial}{\partial y}(y) = \sin(e^x).$$

Partielle Ableitungen: Lösung 5

$$5) \quad f(x, z) = e^{\ln z - xz} = \frac{e^{\ln z}}{e^{xz}} = \frac{z}{e^{xz}} = z \cdot e^{-xz}$$

$$\frac{\partial f}{\partial x} = z e^{-xz} \cdot (-z) = -z^2 e^{-xz}$$

$$\begin{aligned}\frac{\partial f}{\partial z} &= e^{-xz} + z(-e^{-xz})(-x) \\ &= e^{-xz}(1 + xz)\end{aligned}$$

$$\bar{y} = y$$

$$4) f(x,y) = e^{\cos x}$$

$$\frac{\partial f}{\partial x} = e^{\cos x} \cdot \frac{\partial}{\partial x}$$